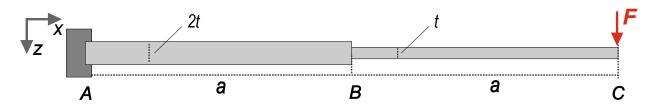
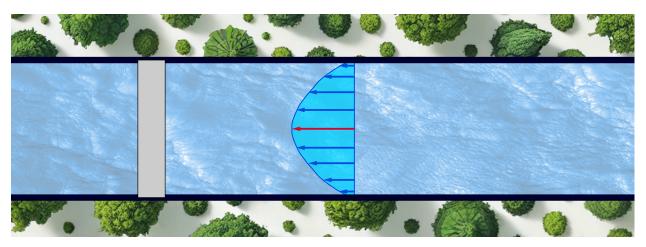
Exercise 9: Beams again 10.01.2025 - 13.01.2025



- (a) Is the problem statically determinate?
- (b) How far from point A is the center of mass of the entire system located?
- (c) What are the reactions and moments at point A?
- (d) Calculate the internal shear forces Q(x) and moments M(x).
- (e) Calculate the deflection profile (bending line) w(x) of the beam. Note! Integration constants are expected to be found, but failing to do so will not result in a large point deduction.



- (a) Write down the expression for v(x) to satisfy the problem formulation.
- (b) From fluid dynamics, we know that at each point, the force q(x) exerted on the net is proportional to the square of the flow speed at that point, v(x). So, $q(x) = \alpha v(x)^2$, where α is a coefficient (dependent on fluid density and drag coefficient, but not important here). Write down the expression for the line load q(x) exerted on the beam.
- (c) Calculate the total load acting on the beam.
- (d) The ends of the beam are fully constrained. Is the problem statically determinate?
- (e) Find the deflection of the beam due to the current, assuming the beam is made of a material with Young's modulus E and its cross-section has a second moment of inertia I. Note! You do not need to solve for the integration constants, but provide the final expression for w(x) with the correct boundary conditions.

Question 3

To celebrate Spring Equinox that will happen in a couple of weeks, group of astronomers decided to decorate their lab with some astronomical memorabilia. To recreate exponential curve that is very important for astronomy, they hanged a lot of thin steel wires with various lengths l(x) on a plastic curtain rod with tubular cross-section, as shown in figure. However, astronomers were not so good in mechanics, so they completely forgot that plastic rod can deform under the weight of steel wires. Help astronomers to sort things out by solving the following problems.

- (a) Calculate the axial moment of inertia I_y for given cross-section with outer diameter d_o and inner diameter d_i .
- (b) Assuming that the wires are very thin, their lengths can be represented as a function of horizontal coordinate x, namely $l(x) = e^{x/a}$. Denoting the linear density (weight per unit of length) of the steel as ρ , write down the expression for line load acting on horizontal beam AB.
- (c) Is the problem statically determinate?
- (d) Find deflection of the beam w(x).
- (e) Determine reaction forces and moments at the beam ends.
- (f) Taking into account the deflection of the beam, do the bottom ends of the steel wires still form an exponential curve?

